SECTION 3.7: Problems

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29. The American coot, Fulica americana, lays clutches of eggs that depend on habitat quality and population density. In a large wetland the distribution of clutch sizes for this species is characterized by the following probability density function:

x (# of eggs)	30.700	8	9	10	11	12
f(x)	0.10	0.10	0.15	0.35	0.25	0.05

- (a) Construct the cumulative density function, F(x), for the pdf above.
- (b) Using the expected value approach, find the mean and variance for the clutch size in this population.
- (c) Find F(10).
- (d) Find P(X = 12).
- (e) Find P(X > 9).
- (f) Find P(X = 12 | X > 9).
- 0. Amazingly, the West Nile virus has been found in more than 200 species of wild vertebrates in North America. Monitoring the spread of this pathogen is difficult but essential. Suppose 10% of a population of American crows in eastern Oklahoma are infected with the virus. How many crows would have to be sampled (analyzed) to be at least 50% certain of finding one infected individual? How many to be 90% certain?
- If the infected and non-infected birds in the preceding problem are binomially distributed, find the following:
 - (a) In a sample of 15 less than 3 will be infected.
 - (b) In a sample of 15 exactly 3 will be infected.
 - (c) In a sample of 15 more than 3 will be infected.